

**【More Exercise】****一、 Multiple Choice**

1. Let  $f(x) = (1 - 2x^3)^{10}$ , then  $f'(1) =$  ( )  
 A. 0    B. -1    C. -60    D. 60
2. If  $f(x) = 2 \ln x - x^2$ , then the solution for  $f'(x) > 0$  is ( )  
 A. (0,1)    B.  $(-\infty, -1) \cup (0, 1)$     C.  $(-1, 0) \cup (1, +\infty)$     D.  $(1, +\infty)$
3. Which of the following equations is incorrect ( )  
 A.  $(3x^2 + \cos x)' = 6x - \sin x$     B.  $(\ln x - 2^x)' = \frac{1}{x} - 2^x \ln 2$   
 C.  $(2 \sin 2x)' = 2 \cos 2x$     D.  $\left(\frac{\sin x}{x}\right)' = \frac{x \cos x - \sin x}{x^2}$
4. The derivative  $y = \frac{5}{x^4 + 3x - 8}$  is ( )  
 A.  $\frac{5}{4x^3 + 3}$     B. 0    C.  $\frac{5(4x^3 + 3)}{(x^4 + 3x - 8)^2}$     D.  $-\frac{5(4x^3 + 3)}{(x^4 + 3x - 8)^2}$
5. Given that the derivative of  $f(x)$  is  $f'(x)$ , and  $f(x) = x^2 + 3xf'(2) + \ln x$ , then the value of  $f'(2)$  is equal to ( )  
 A. 2    B. -2    C.  $\frac{9}{4}$     D.  $-\frac{9}{4}$
6. The tangent line of the function  $y = \frac{x+1}{x-1}$  ( $x \neq 1$ ) is perpendicular to the line  $ax + y + 1 = 0$  at  $(3, 2)$ , therefore, the value of  $a =$  ( )  
 A. 2    B.  $\frac{1}{2}$     C.  $-\frac{1}{2}$     D. -2
7. The derivative of  $y = \log_3 \cos^2 x$  ( $\cos x \neq 0$ ) ( )  
 A.  $-2 \log_3 e \cdot \tan x$     B.  $2 \log_3 e \cdot \cot x$     C.  $-2 \log_3 e \cdot \cos x$     D.  $\frac{\log_2 e}{\cos^2 x}$

**二、 Fill in the blank**

8. The tangible function for  $y = \sin x$  at  $\left(\frac{\pi}{2}, 1\right)$  is \_\_\_\_\_。
10.  $\left(\frac{x^3 - 1}{\sin x}\right)' =$  \_\_\_\_\_,  $[2x \sin(2x + 5)]' =$  \_\_\_\_\_。
11. In a rectangular plane coordinate system  $xOy$ , point P is on the curve C:

$y=x^3-10x+3$  上, and in the second quadrant. Given that the slope of the tangent line of curve C at point P is 2, then the coordinate of point P is \_\_\_\_\_.

### 三、Free Response

12. Given that  $f(x) = \cos x$ ,  $g(x) = x$ , Find the value of  $x$ , so that  $f'(x) + g'(x) \leq 0$

13. (1)  $y = \sin^3 x + \sin x^3$ ; ; find  $y'$

(2) Given that  $f(x) = (x + \sqrt{1+x^2})^{10}$ , find  $\frac{f'(1)}{f(1)}$ 。

14. Find the tangent equation for  $y = \frac{1}{(3x + x^2)^2}$  at  $(1, \frac{1}{16})$ .

15. Given that  $f(x) = x \ln x + \frac{1}{x} e^{x^2}$ ,  $g(x) = f'(x)$ ,  $G(x) = g'(x)$ , Find  $G'(x)$ .